

Switching field distribution of exchange coupled ferri-/ferromagnetic composite bit patterned media

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We investigate the switching field distribution and the resulting bit error rate of exchange coupled ferri-/ferromagnetic bilayer island arrays by micromagnetic simulations. Using islands with varying microstructure and anisotropic properties, the intrinsic switching field distribution is computed. The dipolar contribution to the switching field distribution is obtained separately by using a model of a triangular patterned island array resembling 1.4 Tb/in² bit patterned media. Both contributions are computed for different thickness of the soft exchange coupled ferrimagnet and also for ferromagnetic single phase FePt islands. A bit patterned media with a bilayer structure of FeGd(5 nm)/FePt(5 nm) shows a bit error rate of 10^{-4} with a write field of 1.16 T.

Keywords: exchange-coupled composite media; micromagnetic simulation; ferrimagnet; FEM; bit patterned media; switching field distribution; dipolar interaction field; bit error rate

I. INTRODUCTION

The concept of bit patterned media (BPM) is one of several promising approaches to push data density in magnetic storage devices beyond the limits of conventional perpendicular magnetic recording (PMR)¹⁻³. In this scheme the recording media is an array of decoupled magnetic single domain islands where each dot stores one data bit. While this approach reduces bit transition jitter and improves signal to noise ratio (SNR) compared to PMR⁴, the writeability and thermal stability of the magnetic islands need to be maintained. This can be addressed by designing the islands as exchange spring or exchange coupled composite (ECC) structures which are made of at least two layers of different magnetic anisotropy⁵⁻⁷. In such islands a magnetically hard layer (usually FePt) ensures the thermal stability and an exchange coupled softer layer is used to decrease the required writing field⁸. Ferrimagnetic (FI) materials such as FeGd or FeTb might serve as ideal candidates for the soft layer since their magnetic properties can be tailored easily by their composition. Also in combination with the concept of heat assisted magnetic recording (HAMR), such materials bear potential when exploiting their compensation point.

One of the challenges on the way towards BPM is to

reduce the switching field distribution (SFD) of the island array to ensure a low bit error rate (BER)⁹. The SFD origins of islands can be categorized in intrinsic contributions and stray-field contributions. While the latter deals with the dipolar field interactions between neighbouring islands¹⁰⁻¹², the intrinsic part stems from the variation of magnetic properties, shape and size of the islands¹³⁻¹⁵. Obviously the development of suitable fabrication processes for BPM plays an important role in improving the intrinsic SFD. In this paper, however, we investigate how an exchange-coupled ferrimagnetic layer influences the SFD. Due to the changed magnetization reversal process of exchange spring media and also the amorphous structure of ferrimagnetic materials, this crucial property might be improved significantly^{16,17}. We compute the distributions of the intrinsic and dipolar interaction field contribution separately. To quantify the effect of both contributions, we compute the bit error rate of the medium but neglect other contributions like the head field gradient.

In the following, we briefly present the used micromagnetic model for such bilayer islands and start our investigation by looking at different island diameters and FI-layer thicknesses. We then compute the intrinsic SFD of the bilayer islands by varying the magnetocrystalline anisotropic properties and microstructure of both layers. The dipolar contribution to the SFD is then determined by computing the dipolar interaction field of an array of such islands. Finally we present the results for both contributions and show the influence of the dipolar interaction field on the BER for different island designs.

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II. MICROMAGNETIC SIMULATIONS

Our finite element calculations for the SFD are based on our previously presented model of exchange-coupled ferri-/ferromagnetic heterostructures^{18,19}. Therefore, only a brief summary follows. To calculate the magnetization reversal of the magnetic islands, we use the common Landau-Lifshitz-Gilbert (LLG) equation for ferromagnets (FM) and an adapted LLG equation²⁰ for the ferrimagnetic (FI) layer. The latter is based on the assumption that in thin films the two sub-lattices of the FI are strongly coupled antiparallel and therefore their magnetic moments can be substituted by an effective net moment. This allows the combination of the LLG equation of both sub-lattices to obtain an effective equation for thin FI-layers. For all our simulations the damping constant is set to $\alpha_{\text{eff}} = 1$, since we are only interested in the static hysteresis to extract the switching field H_{sw} .

In the following Section II A we describe how the BER is computed by considering both the intrinsic and the dipolar interaction contribution. Then the respective simulations are described for computing the intrinsic SFD in Section II B and computing the dipolar contribution to the SFD in Section II C. All simulations were performed using the finite element micromagnetic package FEMME²¹.

A. Bit Error Rate of bit patterned media

The intrinsic switching field distribution of the islands can be described with a Gaussian fit, with the mean switching field \bar{H}_{sw} and the standard deviation σ_{int} :

$$f(h) = \frac{1}{\sigma_{\text{int}}\sqrt{2\pi}} e^{-\left(\frac{h-\bar{H}_{\text{sw}}}{\sigma_{\text{int}}\sqrt{2}}\right)^2}. \quad (1)$$

To switch the islands, an external head field \mathbf{H}_{head} is turned on. This field is applied either parallel or tilted with respect to the out-of-plane axis of the medium. For the latter the head field has to be corrected due to the angular variation of the switching field. For single phase islands an effective head field H_{head}^* can be calculated by using the Stoner-Wohlfarth model^{22,23}. Hereby \mathbf{H}_{head} is scaled by a correction function c depending on the angle φ between the applied head field and the anisotropic easy axis of the islands (out-of-plane):

$$c_{\text{sw}}(\varphi) = \left(\sin^{2/3}\varphi + \cos^{2/3}\varphi\right)^{3/2}. \quad (2)$$

Using our micromagnetic model we calculate the switching field of different bilayer systems at different angles φ and also express this angular dependence as correction functions. Later the island designs we investigate will mainly differ in the thickness of the ferrimagnetic (FI) layer t_{FI} , and therefore their corresponding correction function are labelled as $c_{t_{\text{FI}}}$. FIG. 1 shows the analytic Stoner-Wohlfarth correction function c_{sw} in gray

and the simulated correction functions of three island designs with a diameter of $d = 20$ nm and a FI-layer thickness of $t_{\text{FI}} = 0$ nm, 5 nm and 20 nm. The effective head field is calculated by scaling the magnitude of \mathbf{H}_{head} with the respective correction function.

$$H_{\text{head}}^* = c_{t_{\text{FI}}}(\varphi) \|\mathbf{H}_{\text{head}}\| \quad (3)$$

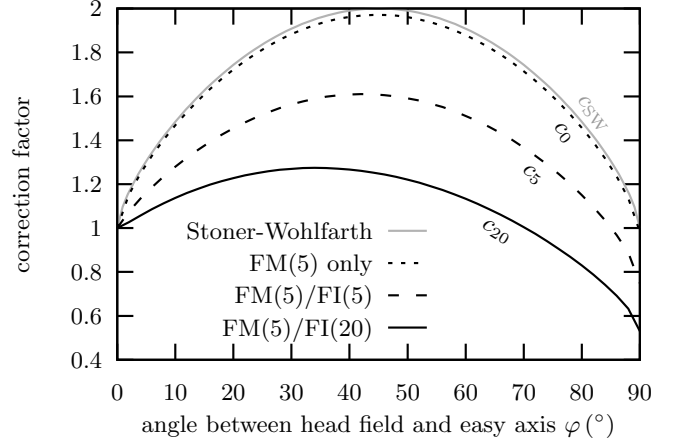


FIG. 1. Correction functions for the angular variation of the switching field. The gray solid curve is the evaluated Stoner-Wohlfarth function c_{sw} in (2). The functions labelled according to the FI-layer thickness of the different island designs c_0 , c_5 and c_{20} are calculated using our micromagnetic model.

The numerically calculated correction function for the single ferromagnetic layer c_0 is very close to the theoretical c_{sw} . When adding the exchange coupled FI-layer the correction factor is generally reduced and even below 1 at higher angles. This means the switching field is less reduced by a tilted head field compared to single phase media or even increases at higher tilting angles. For bilayer islands the maxima of the correction functions move to lower φ . In other words, for soft-hard bilayer structures the minimum switching field resides at lower angles than for single phase islands.

With the respective effective head field as upper limit the probability of switching the islands is given by²⁴:

$$p_{\text{sw}} = \frac{1}{\sigma_{\text{int}}\sqrt{2\pi}} \int_{-\infty}^{H_{\text{head}}^*} e^{-\left(\frac{h-\bar{H}_{\text{sw}}}{\sigma_{\text{int}}\sqrt{2}}\right)^2} dh \quad (4)$$

$$= \frac{1}{2} \left(1 + \text{erf} \left(\frac{H_{\text{head}}^* - \bar{H}_{\text{sw}}}{\sigma_{\text{int}}\sqrt{2}} \right) \right). \quad (5)$$

Therefore, the bit error rate for a set of isolated islands with an intrinsic switching field distribution of σ_{int} is $p_{\text{err}}^{\text{int}} = 1 - p_{\text{sw}}$ or

$$p_{\text{err}}^{\text{int}} = \frac{1}{2} \left(1 - \text{erf} \left(\frac{H_{\text{head}}^* - \bar{H}_{\text{sw}}}{\sigma_{\text{int}}\sqrt{2}} \right) \right). \quad (6)$$

The diagram in Fig. 2 shows the intrinsic distribution $f(h)$ (solid line) and the applied effective field H_{head}^* . Islands with a switching field $H_{\text{sw}} > H_{\text{head}}^*$ (hatched area)

cannot be switched and cause bit errors. The corresponding bit error rate $p_{\text{err}}^{\text{int}}$ is shown as a dashed line.

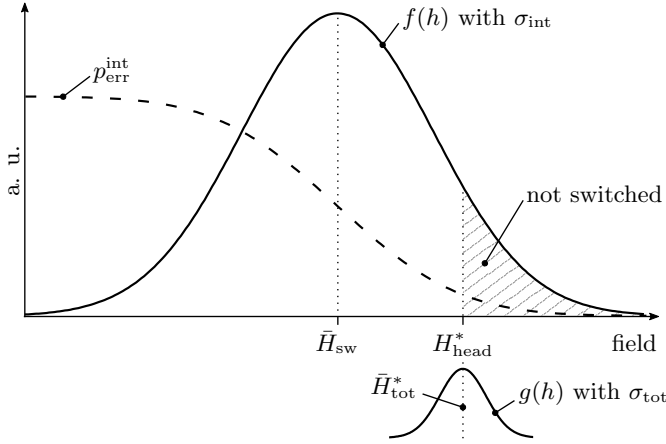


FIG. 2. Schematic of the bit error rate calculation. If the dipolar field is neglected the intrinsic switching field distribution (solid line) and the applied field H_{head}^* determine the bit error rate $p_{\text{err}}^{\text{int}}$ (dashed line) according to (6), since islands with $H_{\text{sw}} > H_{\text{head}}^*$ can not be switched (hatched area). When also taking into account the dipolar field, H_{tot}^* is applied with the distribution of the dipolar field $g(h)$.

However, in arrays of nano islands with increased areal density the magnetostatic dipole interaction between the islands has to be taken into account²⁵. Hence, the field acting on an island is the sum of the current head field and the dipolar interaction field exerted by the neighbouring dots: $\mathbf{H}_{\text{tot}} = \mathbf{H}_{\text{head}} + \mathbf{H}_{\text{dip}}$. Again, either the perpendicular component of the total field can be used²⁶, or it can be corrected by the angular variation of the switching field^{9,27} obtaining a total effective field:

$$H_{\text{tot}}^* = c_{\text{tFI}}(\varphi) \|\mathbf{H}_{\text{head}} + \mathbf{H}_{\text{dip}}\| \quad (7)$$

Here φ is the angle between the total field \mathbf{H}_{tot} and the anisotropic easy axis of the islands. Because the dipolar interaction field is incorporated, the total effective field H_{tot}^* has the distribution of \mathbf{H}_{dip} imprinted. The \mathbf{H}_{dip} acting on an island is determined by the magnetic configuration of the neighbouring islands. By computing \mathbf{H}_{dip} for different randomized magnetic configurations, as described later in section II C, and then calculating H_{tot}^* for each configuration, we get the distribution of the total effective field. This distribution is again approximated by a Gaussian fit:

$$g(h) = \frac{1}{\sigma_{\text{tot}} \sqrt{2\pi}} e^{-\left(\frac{h - \bar{H}_{\text{tot}}^*}{\sigma_{\text{tot}} \sqrt{2}}\right)^2}. \quad (8)$$

Now the previously applied effective field H_{head}^* is substituted by a mean total field \bar{H}_{tot}^* carrying the distribution $g(h)$ (see Fig. 2). By integrating over the product of the total effective distribution $g(h)$ and the bit error rate of isolated islands $p_{\text{err}}^{\text{int}}$, the overall bit error rate $p_{\text{err}}^{\text{tot}}$ can be

computed.

$$p_{\text{err}}^{\text{tot}} = \int_{-\infty}^{\infty} \frac{g(h)}{2} \left(1 - \text{erf}\left(\frac{h - \bar{H}_{\text{sw}}}{\sigma_{\text{int}} \sqrt{2}}\right)\right) dh \quad (9)$$

In this work, especially in section III C, we compare these two different approaches to compute the bit error rate:

- The dipolar interaction field is neglected and therefore an array of isolated islands is assumed. We apply an effective field (3) and calculate $p_{\text{err}}^{\text{int}}$ according to (6).
- The dipolar interaction field is incorporated by imprinting its distribution onto the effective field using (7). The total bit error rate $p_{\text{err}}^{\text{tot}}$ is then calculated according to (9).

In order to obtain the intrinsic distribution and the dipolar interaction field distribution, for both contributions a micromagnetic simulation scheme had to be set up. These two schemes and the used parameters are described in the following subsections II B and II C.

B. Intrinsic switching field distribution

We designed the islands as cylindrical dots with an $L1_0$ chemically ordered $\text{Fe}_{52}\text{Pt}_{48}$ layer as the ferromagnetic (FM) layer and an exchange coupled $\text{Fe}_{74}\text{Gd}_{26}$ layer as the ferrimagnetic (FI) layer. In this arrangement the FM-layer represents the magnetically hard phase which stores the bit while the FI-layer is the magnetically soft phase which helps to lower the switching field and reduce the SFD.

The 5 nm-thick FM-layer has a granular structure with a average grain diameter of 14 nm. Each grain exhibits its own random anisotropy constant and uniaxial anisotropy direction. The easy axes of the grains are within a cone angle of $\theta_{\text{max}} = 15^\circ$. The cone angle defines the maximum deviation of the magneto-crystalline anisotropy axis from the film normal (z -axis). Although the FI-layer is amorphous, we incorporate material inhomogeneities by dividing the layer into patches²⁸ with an average size of 10 nm. Again, the anisotropic properties vary across the patches, but for the FI-layer the uniaxial direction is not confined to a certain cone angle. The thickness of the FI-layer t_{FI} is varied between 3 nm and 50 nm in our simulations. A representation of a bilayer dot with a granular FM-layer and inhomogeneous FI-layer is shown as an inset in Fig. 4. The tessellation of both layers into grains and patches, was generated with the software Neper²⁹.

Since the two layers possess a different microstructure, they are meshed separately. The layers are exchange coupled by calculating the interface exchange energy and incorporating it into the effective field equation of the respective layer. The coupling energy of $J_{\text{ixhg}} = 5 \text{ mJ/m}^2$ between the two layers was chosen to match the coercive

field of experimental data. The exchange constant A_x , the mean anisotropic constant \bar{K}_u , the standard deviation of the anisotropy constant σ_K , the cone angle of the easy axes θ_{\max} and the saturation polarisation J_s of both layers are listed in TABLE I. These values are extracted from experiments and fitting computed magnetization reversal curves to experimentally measured curves. For the material parameters the exchange length $l_x = \sqrt{\mu_0 A_x / J_s^2}$ and the Bloch wall parameter $\delta_0 = \sqrt{A_x / K_u}$ are 2.8 nm and 3.2 nm for FePt and 5.9 nm and 16 nm for FeGd. With a mesh size which is kept always smaller than 2.5 nm we hope to represent domain walls correctly.

TABLE I. Intrinsic magnetic properties of ferri-/ferromagnetic (FI/FM) bilayer islands extracted from experiments.

layer	A_x (pJ/m)	\bar{K}_u (kJ/m ³)	σ_K (%)	θ_{\max} (°)	J_s (mT)
FM (FePt)	10	975	5	15	1257
FI (FeGd)	2	8	20	90	268

The reversal curve of a bilayer island is computed by saturating the island with an applied external field H_{ext} in the positive out-of-plane direction z and then decreasing the field in the opposite direction until the island is switched. The switching field H_{sw} is then obtained by extracting the value of the external field when half of the hard FM-layer is switched, $M_z^{\text{FM}}(H_{\text{sw}}) = 0$. To get the intrinsic SFD we evaluate the reversal curves of one hundred islands. Each island differs only in the randomly generated microstructure and its anisotropic properties within the limits described above. Therefore, other contributions like variation in island diameter or damage due to patterning are not considered.

C. Dipolar interaction field contribution

When looking at the dipolar interaction field we neglect the microstructure of both layers and model an array of equivalent islands, still consisting of two exchange coupled layers, but both layers with perfect out-of-plane anisotropic easy axis. The intrinsic properties A_x , \bar{K}_u and J_s are kept as defined in TABLE I. The array consists of 11×11 islands where, at the center, one island is left out. This gap marks the position where the dipolar interaction field is measured. The dipolar field of these 120 islands is calculated by letting the system relax after randomly assigning an initial magnetization to each island.

To compile a histogram of the interaction field H_{dip} acting on an island we repeat this simulation 500 times, assigning each time a new random initial magnetization, and determine the interaction field H_{dip} at the center of the virtual island (the gap) at the position of the interface between the ferromagnetic and the ferrimagnetic layer. This choice of position is justified by the reversal

mechanism in ECC media, where the critical process is the expansion of a reversed domain into the hard magnetic phase. In our bilayer structure, the ferromagnet (FePt) acts as hard magnetic phase and the ferrimagnet (FeGd) acts as soft phase. The simulation arrangement is illustrated in Fig. 3 with two neighbouring islands, their exerted stray field and the probe point in the gap, where H_{dip} is determined.

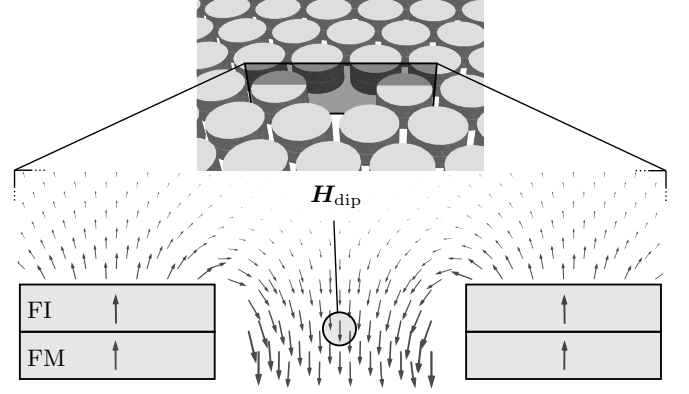


FIG. 3. Schematic of the geometric simulation model to determine the dipolar interaction field acting on an island in an array of bilayer islands.

Of course the dipolar interaction field is strongly dependent on the density and pattern of the array. In this work we investigate an array of islands that are distributed in a triangular pattern. The diameter of the islands is chosen to 20 nm. The triangular patterned array resembles BPM with 1.4 Tb/in² and has a x-pitch of 19.5 nm and a y-pitch of 22.5 nm.

III. RESULTS AND DISCUSSION

To obtain the switching field distribution and the bit error rate of the triangular island arrays, we start by calculating the intrinsic switching field and its distribution in FePt islands and FePt/FeGd bilayer islands. In this island configuration, the FePt layer is the magnetically hard ferromagnet (FM) and the FeGd layer is the soft ferrimagnet (FI). For further investigations we then limit our island configurations to three designs, all with a diameter of $d = 20$ nm:

- FM(5) only: single phase FePt islands with a thickness of $t_{\text{FM}} = 5$ nm.
- FM(5)/FI(5): bilayer islands with equally thick hard and soft phase $t_{\text{FM}} = t_{\text{FI}} = 5$ nm.
- FM(5)/FI(20): bilayer islands with a FePt layer of $t_{\text{FM}} = 5$ nm thickness and a soft FeGd phase with $t_{\text{FI}} = 20$ nm.

With these three configurations, we can compare single phase and exchange coupled composite islands, and also look at an increased FI-layer thickness.

A. Intrinsic switching field distribution

We start our investigation by looking at the switching field and the intrinsic SFD of single islands depending on the thickness of the FI-layer ($t_{\text{FI}} = 0$ to 50 nm). For each value of t_{FI} , the switching fields of 100 islands with randomized microstructure and anisotropic properties, as described earlier in Section II B, are computed. The curves in Fig. 4 show the average of these 100 switching fields depending on t_{FI} for three different island diameters. The standard deviation $\pm\sigma_{\text{int}}$ for the 100 simulation runs is shown as gray shading for each curve and illustrates the intrinsic SFD.

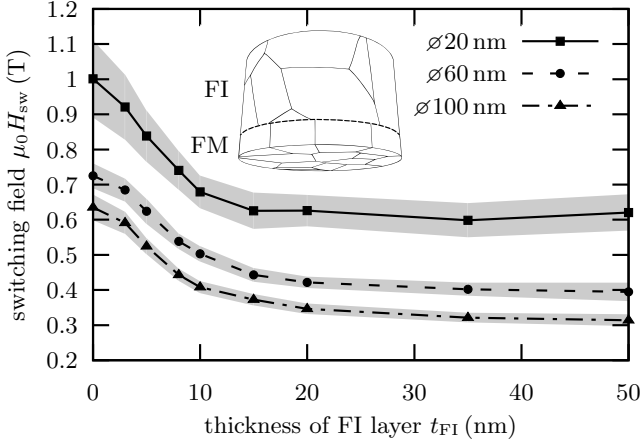


FIG. 4. Mean switching field of bilayer islands depending on the thickness of the FI soft layer for different island diameters (20 nm, 60 nm and 100 nm). Standard deviation of the SFD is depicted as gray shading. The inset shows a typical geometric model of a FM/FI bilayer structure with patches in the FI and columnar grains in the FM-layer.

The switching field decreases with increasing dot diameter. This is due to a change of reversal mechanism from a quasi uniform rotation Fig. 6a to the nucleation and expansion of a reversed domain Fig. 6e. If the thickness of the FI-layer is increased, nucleation and domain wall motion can also be seen for small dot diameters, but only in the soft layer Fig. 6c. The reversal of the hard layer is still by quasi uniform rotation Fig. 6d. Nonuniform reversal modes have a lower nucleation field³⁰. The numerical results show nonuniform reversal of the hard layer for larger diameters. In our previous work¹⁹ we described this behaviour and also the influence of the exchange coupling strength at the interface on the switching field³¹. In this work, however, we will keep the dot diameter at $d = 20$ nm, the interface exchange coupling strength at $J_{\text{ixhg}} = 5 \text{ mJ/m}^2$ and vary the thickness of the FI-layer t_{FI} .

The mean switching field \bar{H}_{sw} decreases with increasing t_{FI} as expected, but only up to a certain value ($t_{\text{FI}} = 15$ nm for $d = 20$ nm) for our set of parameters. This threshold is determined by whether the thickness of the soft ferrimagnetic layer supports the formation of a

domain wall³². We denote t as thickness, K as uniaxial anisotropy constant, J as saturation polarization and A as exchange constant of the magnetically hard ferromagnetic (FM) and the magnetically soft ferrimagnetic (FI) layer with their respective subscript. Then, for very thin soft ferrimagnetic layers the bilayers reverse their magnetization at the nucleation field³³ of

$$H_n = 2 \frac{t_{\text{FM}} K_{\text{FM}} + t_{\text{FI}} K_{\text{FI}}}{t_{\text{FM}} J_{\text{FM}} + t_{\text{FI}} J_{\text{FI}}}. \quad (10)$$

When increasing the thickness t_{FI} , a domain wall is formed in the FI-layer and gets pinned at the interface between the two layers. Therefore the switching field is now determined by the pinning field^{6,34}:

$$H_p = \frac{2K_{\text{FM}}}{J_{\text{FM}}} \frac{1 - \varepsilon_K \varepsilon_A}{(1 + \sqrt{\varepsilon_J \varepsilon_A})^2}, \quad (11)$$

where

$$\varepsilon_K = \frac{K_{\text{FI}}}{K_{\text{FM}}}, \quad \varepsilon_A = \frac{A_{\text{FI}}}{A_{\text{FM}}} \quad \text{and} \quad \varepsilon_J = \frac{J_{\text{FI}}}{J_{\text{FM}}}. \quad (12)$$

The required thickness t_{FI} to form a domain wall in the ferrimagnetic layer is $\delta_{\text{FI}} = \pi \sqrt{A_{\text{FI}} / (J_{\text{FI}} H_p)}$.

In Fig. 5 we compare the demagnetization curves of bilayer islands with diameters $d = 20$ nm and 100 nm and thicknesses of the ferrimagnetic layer of $t_{\text{FI}} = 5$ nm and 20 nm. The thickness of the ferromagnetic layer for all four designs is $t_{\text{FM}} = 5$ nm. Additionally Fig. 6 shows two magnetic configuration states during magnetization reversal for each of the four island designs. The labels on the curves in Fig. 5 correspond to those in Fig. 6.

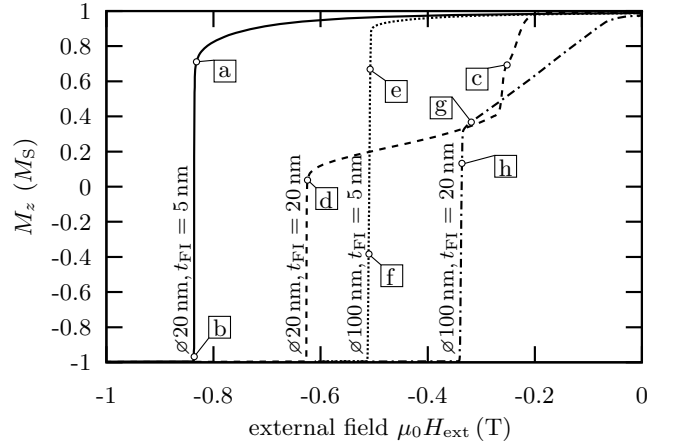


FIG. 5. Demagnetization curves of bilayer islands with diameter $d = 20$ nm and 100 nm and thickness of soft ferrimagnetic layer of $t_{\text{FI}} = 5$ nm and 20 nm. The thickness of the hard ferromagnetic layer is kept constant at $t_{\text{FM}} = 5$ nm. The labels a to h correspond to the magnetic states in Fig. 6, two for each island design.

When considering both, diameter and thickness of the ferrimagnetic layer, we can describe the reversal processes as follows:

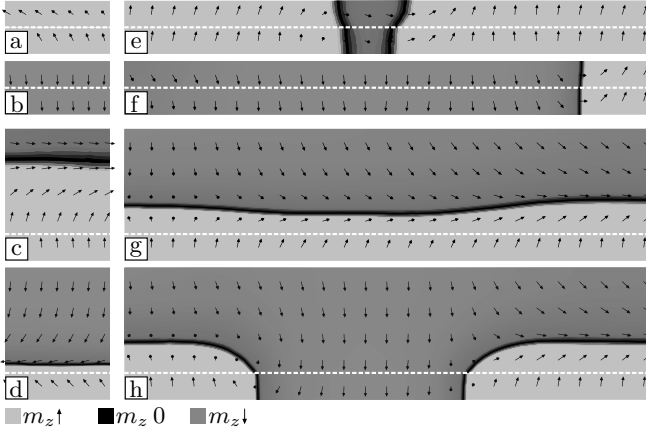


FIG. 6. Magnetic configuration during magnetization reversal of four different bilayer island designs with a t_{FI} thick ferrimagnetic layer on top and a 5 nm thick ferromagnetic layer on the bottom. The interface between the layers is the white dashed line. Left: $d = 20$ nm with $t_{\text{FI}} = 5$ nm (a, b) and $t_{\text{FI}} = 20$ nm (c, d). Right: $d = 100$ nm with $t_{\text{FI}} = 5$ nm (e, f) and $t_{\text{FI}} = 20$ nm (g, h). The labels a to h correspond to the markers in Fig. 5.

- small diameter / thin FI-layer (Figs. 6a and 6b): There is no domain wall formed, the FM-layer reverses coherently in a single step. The FI-layer reduces the switching field, but tightly follows the FM-layer.
- small diameter / thick FI-layer (Figs. 6c and 6d): A domain wall is formed in the FI layer and pushed against the interface with the FM-layer. The latter switches then coherently in a single step.
- large diameter / thin FI-layer (Figs. 6e and 6f): A bubble domain is formed in the FI-layer which then expands into the FM-layer. Both layers are then laterally reversed.
- large diameter / thick FI-layer (Figs. 6g and 6h): A domain wall is formed in the FI-layer and pushed against the interface until the FM-layer switches laterally.

For islands with a diameter of $d = 20$ nm, a 40 % decrease of the mean switching field can be achieved by adding the FI-layer. At the same time this also improves the intrinsic SFD up to a thickness of around $t_{\text{FI}} = 20$ nm but shows a slight increase again above this point. For the case of an island with a diameter of $d = 20$ nm, the hard magnetic layer consists only of two grains whereas the FM layer of an island with $d = 100$ nm is divided in 69 grains. This, of course, leads to a narrower SFD for the larger island, because the overall experienced anisotropy is more uniform from island to island. However, the reduction of the standard deviation due to the added FI-layer is much more pronounced for small diameters.

For our further investigations we choose the smaller islands with $d = 20$ nm, since the larger islands do not

allow for a reasonable areal density of the recording medium. The variation of the FI thickness t_{FI} is reduced to only three variants: no FI-layer at all, $t_{\text{FI}} = 5$ nm and $t_{\text{FI}} = 20$ nm. These values were chosen to compare islands without a coupled ferrimagnetic layer to islands with³⁵ and without a domain wall in the soft magnetic phase during magnetic switching. We fitted the intrinsic SFD of the islands with Gaussian distributions. In Fig. 7 these fits clearly show an improvement of the intrinsic SFD when an exchange coupled ferrimagnetic layer is added. The intrinsic standard deviation is reduced by 59 % for a FI-layer with $t_{\text{FI}} = 20$ nm from $\sigma_{\text{int}} = 110$ mT to $\sigma_{\text{int}} = 45$ mT.

One might argue that a thicker FI-layer improves the SFD at the expense of thermal stability. We calculated the energy barrier of the various dots using the nudge elastic band method³⁶. The results show that the energy barrier for all systems is dominated by the barrier of the hard FePt (FM) layer. The calculated energy barriers are 211 k_BT, 207 k_BT and 234 k_BT for FM(5), FM(5)/FI(5) and FM(5)/FI(20) respectively for $T = 300$ K. This is in qualitative agreement with the results shown by Suess and coworkers³⁷. Hard-soft bilayers islands show a higher attempt frequency than single phase islands^{38,39}. With energy barriers greater than 200 k_BT even high attempt frequencies in the THz-regime give reasonable bit life-times.

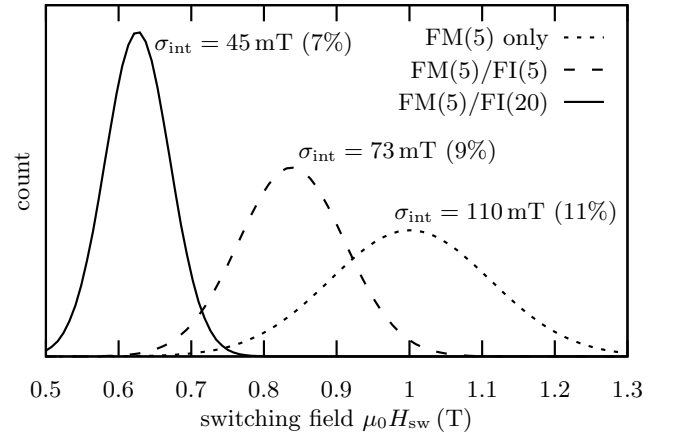


FIG. 7. Reduction of the intrinsic SFD by coupling a FI-layer to a 5 nm thick FM-layer: Gaussian fits for single islands with no FI-layer, 5 nm and 20 nm thick FI-layer. The SFD stems solely from micro-structural variation and the variation of magnetic anisotropy properties of both layers. The standard deviation σ_{int} is given in absolute values and percentage of the respective mean switching field $\mu_0 \bar{H}_{\text{sw}}$.

B. Dipolar interaction field contribution

For the interaction field contribution to the SFD we arrange $d = 20$ nm islands in a triangular pattern of 11×11 bits with a virtual island in the center where the probe

point is located (see inset of Fig. 8). Their microstructure and the anisotropic variation are stripped away and all easy axes are set perfectly out-of-plane. The distribution of the interaction field acting on an island is computed as described in Section II C. Each distribution is compiled from the result of 500 simulation runs with random initial magnetization. Fig. 8 depicts the Gaussian fits of the out-of-plane component of the interaction field distributions h_{dip}^z .

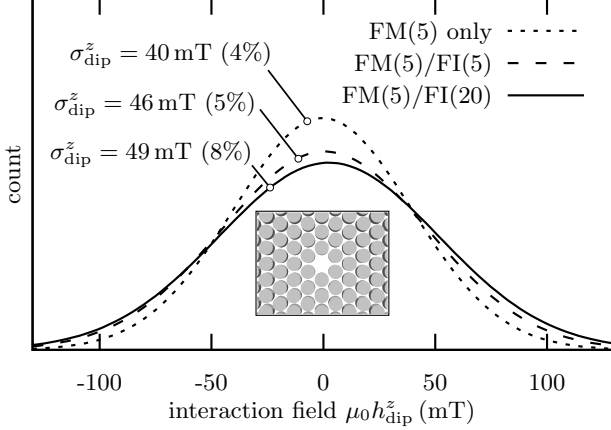


FIG. 8. Gaussian fits of the dipolar interaction field component h_{dip}^z distribution for 11×11 - arrays with triangular island pattern (inset). The distribution is shown for increasing thickness of the FI layer: FM only, 5 nm FI and 20 nm FI on top of FM. The standard deviation σ_{dip}^z is given in absolute values and percentage of the respective mean switching field $\mu_0 \bar{H}_{\text{sw}}$.

In Fig. 9 we show how the angle θ_{dip} between the film normal and the interaction field (see inset) is distributed. We computed the interaction field of 500 random magnetization configurations of the bits in the array and plotted the magnitude of the field as function of the field angle. In general, higher interaction fields can be observed at smaller angles. The results indicate, that in a configuration that leads to an interaction field with a high angle, the field is small. Further we see that most points in Fig. 9 are located in the range from 0° to 20° .

For the calculation of the BER later on, all three orthogonal components of \mathbf{H}_{dip} are considered. Following (7) we compute the distribution of the total field acting on the island from the 500 samples. We again look at islands of single hard FM-layer and bilayer islands with exchange coupled 5 nm and 20 nm thick soft FI-layers. When adding the FI-layer an increase in σ_{dip} of up to 23 % (9 mT) for $t_{\text{FI}} = 20$ nm is observed. This can be attributed to the increased height of the magnetic islands when the FI-layer is added. This change of the island shape increases the stray field acting on a neighbouring island. To test the influence of the number of considered neighbouring islands we did the same calculations for a 17×17 - array. In arrays of bilayer islands with $t_{\text{FI}} = 20$ nm, the maximum deviation was found to be

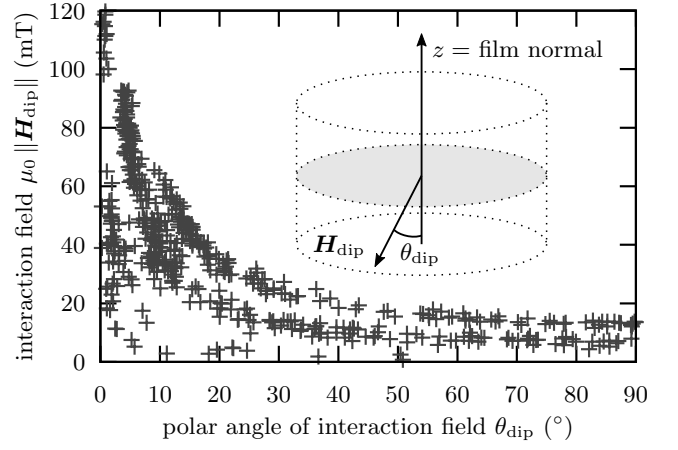


FIG. 9. Magnitude of the interaction field plotted against the respective polar angle θ_{dip} for 500 simulation runs of FM(5 nm)/FI(5 nm) island arrays with random initial magnetization.

0.55 mT for σ_{dip}^z . Therefore we think the choice of 11×11 - arrays is justified.

C. Bit error rate

Generally it can be stated, that adding the FI-layer narrows the intrinsic SFD but broadens the distribution of the interaction field acting on an island. As described in section II A we now calculate the BER with an effective field incorporating the angular variation of the switching field. We do this with and without the dipolar interaction contribution to look at its influence on the BER. The calculations are again done for the three island configurations: single FM-layer with 5 nm thickness and exchange coupled bilayers with 5 nm and 20 nm FI-layer on top of the FM-layer. For this comparison we choose to apply the writing field \mathbf{H}_{head} at two angles $\varphi = 10^\circ$ and $\varphi = 40^\circ$. In Fig. 10 the bit error rates are plotted against the effective head field H_{head}^* .

As shown in section II B, the switching field is decreased when adding the exchange coupled FI-layer. Therefore we see a strong reduction of the BER for a given H_{head}^* with increasing t_{FI} , regardless of the method used to calculate p_{err} . Comparing the two methods $p_{\text{err}}^{\text{int}}$ and $p_{\text{err}}^{\text{tot}}$ we immediately see that incorporating the dipolar interaction field can have a significant impact. The discrepancy between both methods increases when adding an exchange coupled FI-layer because σ_{int} decreases while σ_{dip} , and consequently σ_{tot} , increases slightly and contributes much more. For example, the FM(5)/FI(20) island design at an effective head field of $\mu_0 H_{\text{head}}^* = 838$ mT with $\varphi = 40^\circ$ shows a BER of $p_{\text{err}}^{\text{int}} = 10^{-6}$ without a dipolar field contribution, but a much higher BER of $p_{\text{err}}^{\text{tot}} = 10^{-3}$ when incorporating the interaction field. For $p_{\text{err}}^{\text{int}}$, a change in φ only changes H_{head}^* and therefore does not alter the curves in Fig. 10.

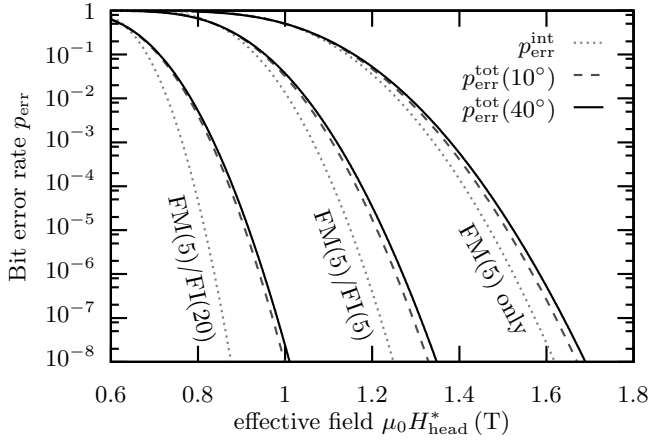


FIG. 10. Calculated bit error rates for single layer islands with no FI-layer and for bilayer islands with 5 nm and 20 nm-thick exchange coupled FI-layer in 1.4 Tb/in² triangular patterned BPM. For all three configurations, the BER without dipolar field contribution $p_{\text{err}}^{\text{int}}$ is shown as dotted line. The BER incorporating the dipolar field contribution $p_{\text{err}}^{\text{tot}}$ in addition is calculated at $\varphi = 10^\circ$ (dashed line) and $\varphi = 40^\circ$ (solid line) head field angle for the three designs.

If the dipolar field is taken into account there is only a neglectable difference for different head field angles.

In TABLE II, the standard deviation for the intrinsic and dipolar contribution to the SFD as well as the switching fields are listed for the three island designs. We also show the respective minimum required effective head field for a given BER of $p_{\text{err}} = 10^{-6}$, with and without incorporating \mathbf{H}_{dip} . From this point of view, if we neglect the interaction field, the required head field for $p_{\text{err}} = 10^{-6}$ and $\varphi = 40^\circ$ is reduced from 1524 mT to 838 mT when a 20 nm FI-layer is added. If we also consider the dipolar field as we proposed, the required field is 951 mT. In other words: When taking the dipolar field into account, we still see a significant reduction of the required writing field, but only by 38% as opposed to the 45% we gain when neglecting \mathbf{H}_{dip} .

D. Read back field

We computed the field above the island at the place where the read head would be positioned. We assumed a magnetic spacing of 6 nm. A map of the perpendicular magnetic field component is shown in Fig. 11. As expected the field decreases with increasing ferrimagnetic layer thickness. This is mostly due to low magnetization of FeGd. The figure also shows the magnetization configurations in the two layers and the vectors of the magnetostatic field. The perpendicular field components $\mu_0 h_{\text{dip}}^z$ are in the range from 10 mT to 40 mT for the thickest ferrimagnetic layer.

TABLE II. Switching field distribution and bit error rate for the three island designs: FM(5) only, FM(5)/FI(5) and FM(5)/FI(20) bilayer. The required effective head fields H_{head}^* are listed for a BER of $p_{\text{err}} = 10^{-6}$ for both calculation methods and two different head field angles $\varphi = 10$ and 40° .

	FM(5)/FI(t_{FI})	(nm)	0	5	20
	σ_{int}	(mT)	110	73	45
	σ_{dip}^z	(mT)	40	46	49
	$\mu_0 \bar{H}_{\text{sw}}$	(mT)	1001	838	626
$p_{\text{err}} = 10^{-6}$	$\mu_0 H_{\text{head}}^*(p_{\text{err}}^{\text{int}})$	(mT)	1524	1186	838
	σ_{tot}	(mT)	46	48	50
	$\mu_0 H_{\text{head}}^*(p_{\text{err}}^{\text{tot}})$	(mT)	1568	1254	941
	σ_{tot}	(mT)	54	54	53
	$\mu_0 H_{\text{head}}^*(p_{\text{err}}^{\text{tot}})$	(mT)	1585	1271	951

^a Angle φ between applied head field and out-of-plane axis.

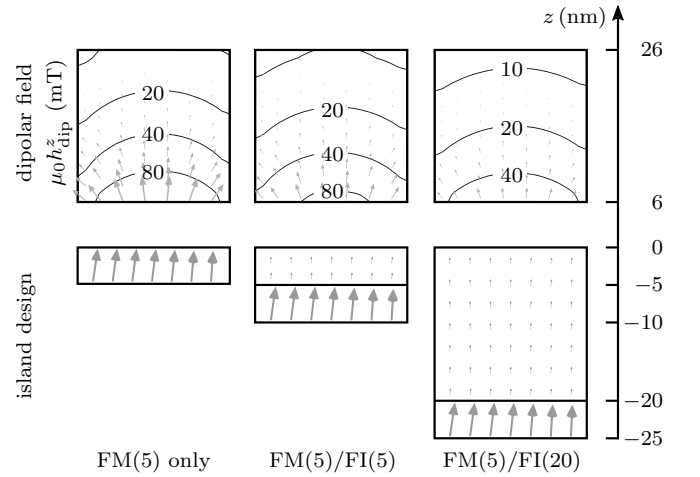


FIG. 11. Calculated stray field (upper boxes) of three single island designs (lower boxes) with a diameter of $d = 20$ nm experienced by a read head with a magnetic spacing of 6 nm. The magnetic moments in the island layers and the stray field above the islands are shown as gray arrows. The isolines in the field boxes show the stray field in mT.

IV. SUMMARY

In this work we described the micromagnetic models to compute the intrinsic contribution and the dipolar interaction field contribution to the switching field distribution (SFD) and switching field of bit patterned media of ferri-/ferromagnetic bilayer islands. A method is proposed to compute the bit error rate (BER) incorporating both contributions and also the angle of the writing field. A decrease of the island diameter (to increase the areal density) changes the reversal mechanism into the single domain regime, and therefore increases the switch-

ing field and broadens the switching field distribution. Our results show that adding an exchange coupled ferrimagnetic (FI) soft layer decreases the switching field and its distribution significantly. This also greatly reduces the bit error rate of bit patterned media. Both the switching field and its distribution decrease with increasing thickness of the ferrimagnetic soft layer, especially up to a thickness which then allows the formation of a domain wall. But with increasing thickness of FI layer and increasing areal density the influence of the dipolar interaction field becomes increasingly important. We conclude that, up to a certain thickness of the soft FI-layer, the bilayer island design is very beneficial for the bit error rate of bit patterned media, but the dipolar field has to be taken into consideration.

In heat assisted magnetic recording bits are addressed for writing by the intersection of the magnetic write field with the heat spot. By careful design of the magnetic write field profile single islands for our chosen dimensions can be addressed⁴⁰. With regard to heat assisted magnetic recording, the exchange coupled ferrimagnetic soft layer should be designed to be at its compensation point, exerting no dipolar interaction field. Only bilayer islands applied with the laser heat spot will have a reduced switching field and will only experience the interaction field of the neighbouring hard phase of the islands. By using this scheme, the advantage of exchange spring media can be exploited while keeping the magnetostatic interaction field low. The method proposed in this work can be used to find the optimal thickness of the FI-layer for certain parameters of head field, head field angle and a desired bit error rate.

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- ¹B. D. Terris, T. Thomson, and G. Hu, *Microsystem Technologies* **13**, 189 (2006).
- ²S. Piramanayagam and K. Srinivasan, *Journal of Magnetism and Magnetic Materials* **321**, 485 (2009).
- ³T. R. Albrecht, H. Arora, V. Ayanoor-Vitikkate, J.-M. Beaujour, D. Bedau, D. Berman, A. L. Bogdanov, Y.-A. Chapuis, J. Cushen, E. E. Dobisz, G. Doerk, He Gao, M. Grobis, B. Gurney, W. Hanson, O. Hellwig, T. Hirano, P.-O. Jubert, D. Kercher, J. Lille, Zuwei Liu, C. M. Mate, Y. Obukhov, K. C. Patel, K. Rubin, R. Ruiz, M. Schabes, Lei Wan, D. Weller, Tsai-Wei Wu, and En Yang, *IEEE Transactions on Magnetics* **51**, 1 (2015).
- ⁴M. Albrecht, C. T. Rettner, A. Moser, M. E. Best, and B. D. Terris, *Applied Physics Letters* **81**, 2875 (2002).
- ⁵R. H. Victora, X. Jianhua, and M. Patwari, *Magnetics, IEEE Transactions on* **38**, 1886 (2002).
- ⁶D. Süß, *Journal of Magnetism and Magnetic Materials* **308**, 183 (2007).

- ⁷A. Goncharov, T. Schrefl, G. Hrkac, J. Dean, S. Bance, D. Suess, O. Ertl, F. Dorfbauer, and J. Fidler, *Applied Physics Letters* **91**, 222502 (2007).
- ⁸R. Sbiaa, K. O. Aung, S. N. Piramanayagam, E.-L. Tan, and R. Law, *Journal of Applied Physics* **105**, 073904 (2009).
- ⁹H. Richter, A. Dobin, O. Heinonen, K. Gao, R. v.d. Veedonk, R. Lynch, J. Xue, D. Weller, P. Asselin, M. Erden, and R. Brockie, *IEEE Transactions on Magnetics* **42**, 2255 (2006).
- ¹⁰O. Hellwig, A. Berger, T. Thomson, E. Dobisz, Z. Z. Bandic, H. Yang, D. S. Kercher, and E. E. Fullerton, *Applied Physics Letters* **90**, 162516 (2007).
- ¹¹B. Pfau, C. M. Günther, E. Guehrs, T. Hauet, T. Hennen, S. Eisebitt, and O. Hellwig, *Applied Physics Letters* **105**, 132407 (2014).
- ¹²V. Repain, *Journal of Applied Physics* **95**, 2614 (2004).
- ¹³T. Thomson, G. Hu, and B. D. Terris, *Physical Review Letters* **96**, 257204 (2006).
- ¹⁴B. Pfau, C. M. Gunther, E. Guehrs, T. Hauet, H. Yang, L. Vinh, X. Xu, D. Yaney, R. Rick, S. Eisebitt, and O. Hellwig, *Applied Physics Letters* **99**, 062502 (2011).
- ¹⁵J. Lee, C. Brombacher, J. Fidler, B. Dymerska, D. Suess, and M. Albrecht, *Applied Physics Letters* **99**, 062505 (2011).
- ¹⁶A. Kikitsu, *Journal of Magnetism and Magnetic Materials* **321**, 526 (2009).
- ¹⁷P. Krone, D. Makarov, T. Schrefl, and M. Albrecht, *Journal of Applied Physics* **109**, 103901 (2011).
- ¹⁸H. Oezelt, A. Kovacs, F. Reichel, J. Fischbacher, S. Bance, M. Gusenbauer, C. Schubert, M. Albrecht, and T. Schrefl, *Journal of Magnetism and Magnetic Materials* **381**, 28 (2015).
- ¹⁹H. Oezelt, A. Kovacs, P. Wohllhüter, E. Kirk, D. Nissen, P. Matthes, L. J. Heyderman, M. Albrecht, and T. Schrefl, *Journal of Applied Physics* **117**, 17E501 (2015).
- ²⁰M. Mansuripur, *The Physical Principles of Magneto-optical Recording* (Cambridge University Press, 1995) pp. 652–654.
- ²¹T. Schrefl, G. Hrkac, S. Bance, D. Süß, O. Ertl, and J. Fidler, in *Handbook of Magnetism and Advanced Magnetic Materials*, edited by H. Kronmüller and S. Parkin (John Wiley & Sons, Ltd, 2007) pp. 1–30.
- ²²A. Shukh, *IEEE Transactions on Magnetics* **40**, 2585 (2004).
- ²³E. C. Stoner and E. P. Wohlfarth, *Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences* **240**, 599 (1948).
- ²⁴H. Muraoka and S. J. Greaves, *IEEE Transactions on Magnetics* **47**, 26 (2011).
- ²⁵H. Muraoka, S. Greaves, and Y. Kanai, *IEEE Transactions on Magnetics* **44**, 3423 (2008).
- ²⁶Y. Dong and R. H. Victora, *IEEE Transactions on Magnetics* **47**, 2652 (2011).
- ²⁷S. Greaves, Y. Kanai, and H. Muraoka, *IEEE Transactions on Magnetics* **44**, 3430 (2008).
- ²⁸M. Mansuripur, R. Giles, and G. Patterson, *Journal of Applied Physics* **69**, 4844 (1991).
- ²⁹R. Quey, P. Dawson, and F. Barbe, *Computer Methods in Applied Mechanics and Engineering* **200**, 1729 (2011).
- ³⁰W. F. Brown, *Journal of Applied Physics* **30**, S62 (1959).
- ³¹T. Hauet, E. Dobisz, S. Florez, J. Park, B. Lengsfeld, B. D. Terris, and O. Hellwig, *Applied Physics Letters* **95**, 262504 (2009).
- ³²F. B. Hagedorn, *Journal of Applied Physics* **41**, 2491 (1970).
- ³³R. Skomski and J. M. D. Coey, *Physical Review B* **48**, 15812 (1993).
- ³⁴H. Kronmüller and D. Goll, *Physica B: Condensed Matter* **319**, 122 (2002).
- ³⁵A. Y. Dobin and H. J. Richter, *Journal of Applied Physics* **101**, 09K108 (2007).
- ³⁶R. Dittrich, T. Schrefl, D. Suess, W. Scholz, H. Forster, and J. Fidler, *Journal of Magnetism and Magnetic Materials* **250**, 12 (2002).
- ³⁷D. Suess, T. Schrefl, S. Fähler, M. Kirschner, G. Hrkac, F. Dorfbauer, and J. Fidler, *Applied Physics Letters* **87**, 012504 (2005).
- ³⁸J. Dean, M. A. Bashir, A. Goncharov, G. Hrkac, S. Bance,

- T. Schrefl, A. Cazacu, M. Gubbins, R. W. Lamberton, and D. Suess, [Applied Physics Letters](#) **92**, 142505 (2008).
- ³⁹R. Victora and Xiao Shen, [Proceedings of the IEEE](#) **96**, 1799 (2008).
- ⁴⁰A. Kovacs, H. Oezelt, M. E. Schabes, and T. Schrefl, [Journal of Applied Physics](#) **120**, 013902 (2016).